

## Key

1. Explain how currying works.<sup>1</sup>

Currying involves taking an n-place function and breaking it down into a sequence of n-many 1-place functions.

2. Fill in the blank spots

$$(1) \quad \{ x \in D \mid \{ y \in D \mid y \text{ saw } x \} \}$$

$$f : D \rightarrow \{ g \mid g : D \rightarrow \{ 1, 0 \} \}$$

for all  $x \in D$ ,  $f(x) =$

$$g : D \rightarrow \{ 1, 0 \}$$

for all  $y \in D$ ,

$$g(y) = 1 \text{ iff } y \text{ saw } x$$

$$\lambda x \in D. \lambda y \in D. \text{saw}(x)(y)$$

$$(2) \quad \{ x \in D \mid \{ z \in D \mid z \text{ knows } x \} \}$$

$$f : D \rightarrow \{ g \mid g : D \rightarrow \{ 1, 0 \} \}$$

for all  $x \in D$ ,  $f(x) =$

$$g : D \rightarrow \{ 1, 0 \}$$

for all  $z \in D$ ,

$$g(z) = 1 \text{ iff } z \text{ knows } x$$

$$\lambda x \in D. \lambda z \in D. \text{knows}(x)(z)$$

$$(3) \quad \{ x \in D \mid \{ y \in D \mid y \text{ likes } x \} \}$$

$$f : D \rightarrow \{ g \mid g : D \rightarrow \{ 1, 0 \} \}$$

for all  $x \in D$ ,  $f(x) =$

$$g : D \rightarrow \{ 1, 0 \}$$

for all  $y \in D$ ,

$$g(y) = 1 \text{ iff } y \text{ likes } x$$

$$\lambda x \in D. \lambda y \in D. \text{likes}(x)(y)$$

3.  $\beta$ -Convert each of the following  $\lambda$ -expressions (*i.e.* give the result of plugging in these arguments). Then, give the English expression that corresponds to that result.

$$1. [\lambda z \in D. \lambda y \in D. \text{hugged}(z)(y)](\text{Asia})(\text{Yolanda})$$

$$\text{hugged}(\text{Asia})(\text{Yolanda}) ; \text{Yolanda} \text{ hugged Asia}$$

$$2. [\lambda x \in D. \lambda y \in D. \text{called}(x)(y)](\text{Imogen})(\text{Barry})$$

$$\text{called}(\text{Imogen})(\text{Barry}) \text{ Barry called Imogen}$$

4. Write the denotations of the following English expressions as functions, using the  $\lambda$ -notation.

$$1. \text{smash}$$

$$\lambda x \in D. \lambda y \in D. \text{smash}(x)(y)$$

$$2. \text{carry}$$

$$\lambda x \in D. \lambda y \in D. \text{carry}(x)(y)$$

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<sup>1</sup>or: Explain how schönfinkelization works.